PERFORMANCE OF AXIAL-FLOW FAN AND COMPRESSOR
BLADES DESIGNED FOR HIGH LOADINGS
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SUMMARY

An investigation to determine the effects of loading on the performance of axial-flow fan and compressor blades was carried out in a test blower. The performance of four sets of rotor blades, designed to set up free vortex flow and operating with design pitch-section lift coefficients from 0.31 to 0.99, was studied by making surveys of yaw angles and pressures.

Blades designed for loadings higher than those now in use gave peak efficiencies of approximately 96 percent; a decided decrease in peak efficiency occurred for very low loading. For blades with a solidity of 1.0, design lift coefficients approaching 1.0 can be used with high efficiencies and a maximum lift coefficient of at least 1.4 can be obtained.

The measured performance was very close to that predicted from studies of stationary two-dimensional cascades in NACA ACR No. L5F07e: the blade peak efficiency was close to the design point for high loadings, turning angles were within 1° of predicted angles, and at design conditions, 92 to 95 percent of the ideal pressure rise was obtained.

Extreme leading-edge roughness caused a 2.5- to 3-percent decrease in efficiency and an 11- to 15-percent drop in pressure rise at the design conditions.
INTRODUCTION

Investigations of stationary two-dimensional blade cascades to obtain design data for high-pressure-rise and high-efficiency axial-flow compressors and fans are reported in references 1 and 2. Conditions for these stationary tests, however, could not exactly simulate those for rotating blades and no information on efficiency or range was obtained. Tests were conducted, therefore, on four rotors with blades of different loadings designed from the data of reference 2. The blades, designed to set up free vortex flow, operated with design lift coefficients at the pitch section from 0.31 to 0.99. From surveys of angles and pressures before and after the blades, the effects of loading on compressor performance were evaluated. The actual three-dimensional flows were compared with the two-dimensional flows. The tests were made in a single-stage test blower at the Langley Memorial Aeronautical Laboratory of the NACA.

SYMBOLS

\( A \) \quad \text{annulus area, square feet}
\( c_l \) \quad \text{blade-section lift coefficient}
\( c_p \) \quad \text{specific heat of air at constant pressure, foot-pounds per slug per } ^\circ\text{F}
\( D \) \quad \text{diameter, feet}
\( H \) \quad \text{total pressure, pounds per square foot}
\( \Delta H \) \quad \text{weighted-average total-pressure rise, pounds per square foot}
\( n \) \quad \text{rotor speed, revolutions per second}
\( p \) \quad \text{static pressure, pounds per square foot}
\( \Delta p \) \quad \text{static-pressure rise, pounds per square foot}
\( Q \) \quad \text{quantity flow, cubic feet per second}
q  dynamic pressure, pounds per square foot
T  temperature, °F absolute
U  rotational velocity of rotor blade element at any
    radius, feet per second
V  velocity of air relative to casing, feet per
    second
W  velocity of air relative to rotor, feet per
    second
Δw change in tangential velocity, feet per second
    (measured parallel to blade row)
α  effective angle between entering air and chord line,
    degrees
α₀ angle between mean air and chord line, degrees
β effective stagger angle, degrees (angle of entering
    air measured from axial direction)
β₀ mean stagger angle, degrees (angle of mean air
    measured from axial direction)
δ  ratio of change in tangential velocity Δw to
    axial velocity Vₐ
η  adiabatic rotor efficiency evaluated from surveys
    1/2 chord upstream and 1/2 chord downstream
    from rotor
θ  effective angle through which air is turned
    relative to rotor, degrees
ρ  mass density, slugs per cubic foot
φ  angle through which air is turned relative
    to casing, degrees
\[ \sigma \] solidity (blade chord divided by gap between blades or number of blades times chord divided by circumference)

\[ \Delta p/q_o \] section pressure-rise coefficient based on mean dynamic pressure

\[ \frac{p - p_{atm}}{\frac{1}{2} \rho U_t^2} \] local static-pressure coefficient

\[ \frac{\Delta H}{\frac{1}{2} \rho U_t^2} \] fan total-pressure-rise coefficient

\[ \frac{H - p_{atm}}{\frac{1}{2} \rho U_t^2} \] local total-pressure coefficient

\[ \frac{Q}{nD_t^3} \] quantity coefficient

Subscripts

\( o \) mean-air conditions (one-half vector sum of entering and leaving values)

\( l \) entering rotor

\( 2 \) leaving rotor

\( a \) axial direction

\( atm \) atmospheric conditions

\( p \) pitch section (midway between root and tip sections)

\( s \) stagnation

\( t \) tip
DESCRIPTION OF APPARATUS

Test blower.—All tests were made in the single-stage test blower shown in figures 1 and 2. The tip diameter was 27.82 inches and the hub diameter was 21.82 inches; the hub-to-tip ratio was therefore 0.78. The 26-blade rotor was driven directly by a 75-horsepower motor with a speed range from 0 to 3600 rpm. Because of power limitations, the tests were made at speeds from 2000 to 2400 rpm. No guide vanes or stator blades were used since the primary purpose of the investigation was to obtain blade characteristics, which were most simply obtained by testing a rotor only.

The air enters through eight radial ports, the areas of which may be changed by sliding plates, and then passes through a 60-mesh screen and two 30-mesh screens supported on \( \frac{1}{4} \)-inch screens. These screens smooth out the variations in the flow caused by the inlet. The converging section accelerates the flow to the velocity desired in the straight test section with very small boundary layers. Surveys of the total and static pressures and of the yaw angles were made \( \frac{1}{2} \) chord upstream and \( \frac{1}{2} \) chord downstream from the rotor-blade leading edge and trailing edge, respectively. A survey instrument with a measuring head that contains yaw, static-pressure, and total-pressure tubes was used. The instrument and its installation are shown in figure 3. Approximately 12 inches behind the rear survey station, the air enters an annular diffuser that exhausts to the atmosphere.

Blades.—The blades for the tests were designed to set up free vortex flow by use of blade section data from reference 2. Such blading gives a constant total-pressure rise along the blade and a variation of absolute tangential velocity of the flow that is inversely proportional to the radius. These conditions theoretically result in a constant axial velocity through the blades for incompressible flow and constant flow area. (See typical vector diagram, fig. 4(a).) Since the variation of these conditions along the blade is known, if conditions are fixed at one section they may be evaluated at all others. The arbitrary choice of the number of blades and the blade plan form fixes the solidity at all sections. With the variables — stagger, turning angle, and solidity — known,
the design charts of reference 2 can be used to find profiles and settings for the desired flow.

For the test blades, the basic vector diagram at the pitch section was set up by choosing $\beta_0 = 45^\circ$ so that the performance of the four blades could be compared for the same mean flow. The root, pitch, and tip sections were designed and the blade was completed by fairing between these sections. A solidity of 1.0 was chosen at the pitch section and, for simplicity of construction, the blade chord was kept constant at 3 inches. For convenience, the blades are designated by the value at the pitch section of the ratio of change in tangential velocity to axial velocity $\delta$ (nondimensional measure of the blade loading). The blades tested, $\delta = 0.2$, 0.4, 0.6, and 0.7, are shown in figure 5. Design information for the four sets of blades are presented in table I. An error in construction of the 0.2 blade resulted in a twist approximately 10° less than the design twist. Although this error gives a small deviation from vortex flow, the effects on performance should be small.

The clearance between the tip of the blades and the casing was 0.007 ± 0.002 inch. There were also gaps of approximately 0.007 ± 0.002 inch between the overhanging part of the root section of the blade and the rotor surface, as well as small stress-relief cut-outs at the root-hub juncture. (See fig. 5.)

TESTING TECHNIQUE

All tests were made for a range of quantity flow from the maximum obtainable to that at which stall occurred with the blades set at their respective design angles. This stall is defined as the condition at which the mass flow through the rotor suddenly decreased. No data were taken in the stalled condition. No flows higher than design could be obtained from the 0.2 blades because of the combination of low pressure rise and throttling effect of the entrance ports and screens.

The 0.2, 0.4, and 0.6 blades were tested at 2400 rpm, but because of power limitations the 0.7 blades were tested at 2000 rpm. A few tests of the 0.6 blades at both speeds showed no noticeable change in performance. Blade roughness was simulated by placing a strip of
1/4-inch masking tape along the entire leading edge
(1/4 inch on each surface) of the 0.4 and 0.7 blades for
a few tests. This roughness is believed to be more severe
than the roughness that would be encountered in practice.
The tests were run at Reynolds numbers of approximately
300,000 to 500,000 and corresponding Mach numbers of
approximately 0.20 to 0.26, based on blade chord and mean-
air conditions relative to the rotor.

Readings of yaw angle and static and total pressures
upstream and downstream from the rotor were taken at
26 radial positions across the annulus. The yaw angle
was obtained by the "null" method; that is, the measuring
head was rotated until the two yaw tubes registered equal
pressures and then the angle was read with a vernier on
the protractor scale. The yaw head was calibrated to
within 10.10 and consecutive tests gave a precision of
10.25° for turning angles. Close to the tip and hub,
where the flow is rough, the precision decreases to
approximately 10.4°. A calibration test showed that no
correction to the static- or total-pressure readings was
required at the test velocities. The micrometer drive of
the survey apparatus allowed an accuracy of radial
settings to 10.001 inch. Static and total pressures were
measured on an alcohol manometer to 10.03 inch and speed
was held constant to within 13 rpm. Readings of air
temperature were taken at the start, in the middle, and
at the end of the test; barometer and humidity readings
were taken only once during the test.

Since the measured yaw angles were based on stationary
coordinates, the turning angles, which are based on rotor
coordinates, were calculated from these angles, the
measured velocities upstream and downstream from the rotor,
and the known velocity of the blade element. Since the
inlet velocity was axial, power input was obtained from

$$\int \Delta F \left( \rho_2 V_{a2} \Delta \omega \right) dA$$

the values of $\rho_2$, $V_{a2}$, and $\Delta \omega$ measured at each of
the 26 points of the radial survey being used. This method of measuring power input is shown to agree with motor-torque measurements to better than 1 percent in a British paper of limited circulation.

Power output was obtained from

$$\int_A c_p \left( \rho_2 V_2 T_2 - \rho_1 V_1 T_1 \right) dA$$

by using calculated adiabatic stagnation temperatures corresponding to the measured total pressures of the radial surveys. The efficiency, obtained by dividing the power output by the power input, had a precision of ±0.6 percent for the 0.4, 0.6, and 0.7 blades. The precision decreased to ±1.0 percent for the 0.2 blades because of the very low power involved. The accuracy of the measurements for individual tests was established by requiring that the mass flows obtained from integration of data obtained upstream and downstream from the rotor agree to within one-half of 1 percent. This efficiency is a rotor efficiency and should not be compared directly with stage efficiencies.

RESULTS AND DISCUSSION

Effects of blade loading.— The efficiency curves (fig. 6) show the high efficiency of the highly loaded blades. The three most highly loaded blades had peak efficiencies of approximately 96 percent whereas the most lightly loaded blade had a peak efficiency of only 92.7 percent. At the same time, high efficiency was obtained over a wide range of quantity coefficient. The available range of quantity coefficient of the four blades, both for a 5-percent decrease in efficiency and from design condition to blade stall, is presented in the following table:
The efficiency contours, superimposed on the pitch-section lift curves (fig. 7), show that lift coefficients as high as 1.0 at a solidity of 1.0 may be realized with very high efficiency. From the lift curves (fig. 8), it is apparent that a maximum lift coefficient of 1.0 at a solidity of 1.0 (suggested as the limit, but not attained, in reference 3) is well exceeded. Thus, the use of available cascade results and the design charts of reference 2 permit the design of blades with loadings higher than those now in use with assurance that high efficiency can be obtained. The fan total-pressure curves for the four blades are presented in figure 9. High-speed tests of these highly cambered blades are being made by the NACA to determine the effects of compressibility on performance. The pressure ratio estimated for the 0.7 blade without entrance vanes at a tip speed of approximately 750 feet per second (below the predicted blade critical speed) is, however, as high as experimental values obtained with present-day blades operating at tip speeds near 1000 feet per second (reference 4). With entrance vanes and comparable tip speeds, the estimated pressure rise is 50 percent higher than the highest now obtained. The increased blade loadings will permit the design of high-performance compressors which will be light and short since the desired pressure rise can be obtained in fewer stages.
The pitch section of the 0.7 blade reaches a lift coefficient of almost 1.2 (fig. 8), and the hub section of this blade was found to reach a lift coefficient of approximately 1.4 before stall. Even the maximum lift coefficient of 1.4 could probably be increased since the section at the root of the 0.7 blade was not the maximum camber section recommended in reference 2. The data on maximum lift coefficient obtained for the pitch section of the four blades are summarized in the following table:

<table>
<thead>
<tr>
<th>Blade-designation</th>
<th>Design ( c_{l0} ) for pitch section</th>
<th>Maximum ( c_{l0} ) for pitch section</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>0.31</td>
<td>0.78</td>
</tr>
<tr>
<td>0.4</td>
<td>0.61</td>
<td>0.91</td>
</tr>
<tr>
<td>0.6</td>
<td>0.86</td>
<td>1.09</td>
</tr>
<tr>
<td>0.7</td>
<td>0.99</td>
<td>1.19</td>
</tr>
</tbody>
</table>

Verification of two-dimensional design data. — The design point is defined as the point at which each blade section is operating at the angle of attack obtained from the two-dimensional blade-section design charts of reference 2. This design point is indicated by a short bar across the curves on the figures that show blade and section characteristics.

The investigation shows that the measured performance is very close to the design performance. The design points on the efficiency curves of figure 6 show the validity of the design procedure and of the assumption of reference 2 that maximum efficiency would be obtained if the blade pressure distribution were free from peaks. For all of the blades except the most lightly loaded, the design point falls very close to the peak efficiency.

The surveys of turning angles near the design points of the four blades (figs. 10 to 13) show that the measured angles agree with the predicted angles to within 1° over most of the blade span. This close agreement permits the calculation of power absorbed by a set of blades to within a few percent. The difference between turning angles with respect to the rotor and with respect to the casing is shown by a comparison of figures 12 and 14. The points in figure 12 were calculated from the measured values shown in figure 14. A cross plot of the turning-angle surveys at the pitch section is shown in figure 15.
The static-pressure rise at design conditions (fig. 16) was found to be 92 to 95 percent of the ideal values for which losses are neglected. It may be noted that, as the loading is increased, the design point moves closer to the maximum pressure rise.

Since the blades were designed to set up free vortex flow, the axial velocities ahead of and behind the rotor should be equal and the total-pressure rise along the blade should be constant. The axial-velocity distribution obtained near design condition (fig. 17) is very close to the ideal uniform distribution over the part of the blade span not affected by the hub and tip. The pressure-coefficient curves (fig. 18) also show the desired constant total-pressure increase over the part of the blade not affected by the hub and tip disturbances. The entrance flow has almost constant static and total pressures and shows that the wall boundary layers entering the rotor are very small.

Effects of blade roughness.—Simulated blade roughness caused decreases in efficiency of 2.5 to 3 percent, which changed but little with loading. A decrease in turning angle of approximately 0.6° for the 0.4 blades and 2° for the 0.7 blades is noticeable over most of the blade length (figs. 11 and 13.) This decrease, plus the increased losses due to roughness, caused decreases of 11 to 15 percent and 8 to 13 percent in pressure-rise and lift coefficient, respectively (figs. 16 and 8). The losses in efficiency, pressure rise, and turning angle are sufficient to warrant close attention to the surface in the vicinity of the blade nose and perhaps cleaning of the blades at intervals during operation.

CONCLUSIONS

As a result of the series of tests made on four sets of blades of different loadings in a single-stage test blower to determine the effects of loading on the performance of axial-flow fan and compressor blades, the following conclusions were reached:

1. Blades designed for loadings higher than those now in use gave peak efficiencies of approximately 96 percent; a decided decrease in peak efficiency occurred
for very low loading. For blades with a solidity of 1.0, 
design lift coefficients approaching 1.0 can be used with 
high efficiencies and a maximum lift coefficient of at 
least 1.4 can be obtained.

2. The measured performance was very close to that 
predicted from studies of stationary two-dimensional 
cascades given in NACA ACR No. L5F03a: the blade peak 
efficiency was close to the design point for high loadings, 
turning angles were within 1° of predicted values, and at 
design conditions 92 to 95 percent of the ideal pressure 
rise was obtained.

3. Extreme leading-edge roughness caused a 2.5- to 
3-percent decrease in efficiency and an 11- to 15-percent 
decrease in pressure rise at the design conditions.

Langley Memorial Aeronautical Laboratory 
National Advisory Committee for Aeronautics 
Langley Field, Va., April 19, 1946

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3. Keller, Curt.: The Theory and Performance of Axial- 
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### TABLE I. - BLADE DESIGN DETAILS

[Blower-blade sections and settings obtained from fig. 41 of reference 2]

<table>
<thead>
<tr>
<th>Section</th>
<th>$\beta$ (deg)</th>
<th>$\theta$ (deg)</th>
<th>$\sigma$</th>
<th>Blower-blade section</th>
<th>$\alpha$ (deg)</th>
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</thead>
<tbody>
<tr>
<td>Root</td>
<td>44.0</td>
<td>7.6</td>
<td>1.135</td>
<td>65-(3.25)10</td>
<td>a7.8</td>
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<tr>
<td>Pitch</td>
<td>48.0</td>
<td>6.0</td>
<td>1.000</td>
<td>65-(3.00)10</td>
<td>6.2</td>
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<tr>
<td>Tip</td>
<td>51.0</td>
<td>4.4</td>
<td>0.892</td>
<td>65-(2.50)10</td>
<td>b5.1</td>
</tr>
</tbody>
</table>

$\delta = 0.2$ blade

<table>
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<tr>
<th>Section</th>
<th>$\beta$ (deg)</th>
<th>$\theta$ (deg)</th>
<th>$\sigma$</th>
<th>Blower-blade section</th>
<th>$\alpha$ (deg)</th>
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<tbody>
<tr>
<td>Root</td>
<td>46.5</td>
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<td>1.135</td>
<td>65-810</td>
<td>11.9</td>
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<tr>
<td>Pitch</td>
<td>50.2</td>
<td>11.5</td>
<td>1.000</td>
<td>65-710</td>
<td>10.2</td>
</tr>
<tr>
<td>Tip</td>
<td>53.9</td>
<td>8.5</td>
<td>0.892</td>
<td>65-610</td>
<td>8.4</td>
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$\delta = 0.4$ blade

<table>
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<tr>
<th>Section</th>
<th>$\beta$ (deg)</th>
<th>$\theta$ (deg)</th>
<th>$\sigma$</th>
<th>Blower-blade section</th>
<th>$\alpha$ (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Root</td>
<td>48.8</td>
<td>24.1</td>
<td>1.135</td>
<td>65-(13.5)10</td>
<td>16.7</td>
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<tr>
<td>Pitch</td>
<td>52.4</td>
<td>17.4</td>
<td>1.000</td>
<td>65-(11)10</td>
<td>13.1</td>
</tr>
<tr>
<td>Tip</td>
<td>55.5</td>
<td>12.9</td>
<td>0.892</td>
<td>65-(8.5)10</td>
<td>10.0</td>
</tr>
</tbody>
</table>

$\delta = 0.6$ blade

<table>
<thead>
<tr>
<th>Section</th>
<th>$\beta$ (deg)</th>
<th>$\theta$ (deg)</th>
<th>$\sigma$</th>
<th>Blower-blade section</th>
<th>$\alpha$ (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Root</td>
<td>49.9</td>
<td>28.6</td>
<td>1.135</td>
<td>65-(16.5)10</td>
<td>18.3</td>
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<tr>
<td>Pitch</td>
<td>53.5</td>
<td>20.4</td>
<td>1.000</td>
<td>65-(12.75)10</td>
<td>14.9</td>
</tr>
<tr>
<td>Tip</td>
<td>56.5</td>
<td>14.9</td>
<td>0.892</td>
<td>65-(10.5)10</td>
<td>12.0</td>
</tr>
</tbody>
</table>

$\delta = 0.7$ blade

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<sup>a</sup>Actual construction, 7.3.

<sup>b</sup>Actual construction, 5.6.
Figure 1.- Schematic diagram of single-stage test blower.
Figure 2.- Three-quarter rear view of the single-stage test blower with top half of test section removed.
Figure 3. - Installation and close-up of survey instruments and measuring head.
(a) Constant axial velocity.

(b) Varying axial velocity.

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Figure 4.- Typical vector diagrams for axial-flow fans and compressors.
Figure 5. - Blades from each of the four rotors tested.
Figure 6.- Variation of efficiency with quantity coefficient for the four blades tested. Efficiency is calculated from surveys and only rotor losses are included. (Dashed vertical lines show design points; flagged symbols designate tests with roughness.)
Figure 7.—Measured variation of efficiency with pitch-section lift coefficient. Efficiency is calculated from surveys and only rotor losses are included. (Short bars across curves are design points.)
Figure 8.—Variation of lift coefficient at the pitch section for the four blades tested. (Short bars across curves are design points; flagged symbols designate tests with roughness.)
Figure 9. - Variation of fan weighted-average total-pressure-rise coefficient with quantity coefficient for the four blades tested. (Short bars across curves are design points; flagged symbols designate tests with roughness.)
Figure 10. - Variation of turning angle along the $S = 0.2$ blade and comparison with angles predicted from reference 2. Design conditions: $\alpha_p = 6.2^\circ$, $\frac{Q}{nD_c^3} = 0.712$. 

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Figure 11. - Variation of turning angle along the $\delta = 0.4$ blade - including one test with roughness - and comparison with angles predicted from reference 2.

Design conditions: $\alpha_p = 10.2^\circ$; $\frac{Q}{nD_t^3} = 0.625$. 

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Figure 12.- Variation of turning angle along the $S = 0.6$ blade and comparison with angles predicted from reference 2. Design conditions: $\alpha_p = 13.1^\circ$, $\frac{Q}{nD_t^3} = 0.604$. 

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Figure 13.—Variation of turning angle along the \( \delta = 0.7 \) blade — including one test with roughness — and comparison with angles predicted from reference 2. Design conditions: \( \alpha_p = 14.9^\circ; \frac{Q}{nD_t^3} = 0.598 \).
Figure 14: Variation of measured angle with respect to the casing along the $\delta = 0.6$ blade for four test conditions. Design conditions: $\alpha_p = 13.10^\circ$, $\frac{Q}{nD_t^3} = 0.604$. 
Figure 15.- Variation of turning angle at the pitch section for the four blades tested. (Short bars across curves are design points.)

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Figure 16. - Variation of section pressure-rise coefficient at the pitch section for the four blades tested. (Short bars across curves are design points; flagged symbols designate tests with roughness.)
Figure 17. — Axial-velocity surveys upstream and downstream from the $e = 0.6$ blade over a range of quantity coefficient. Design conditions: $a_p = 13.1^\circ; \frac{Q}{nD^3} = 0.60$. 

NACA 1201
Figure 18. - Typical pressure survey showing variation of static and total pressures along the \( \delta = 0.6 \) blade.

\[ \alpha_p = 1210; \quad \frac{Q}{nD_t^3} = 0.629. \]