SOME INVESTIGATIONS OF THE GENERAL INSTABILITY
OF STIFFENED METAL CYLINDERS
IV - CONTINUATION OF TESTS OF SHEET-COVERED SPECIMENS
AND STUDIES OF THE BUCKLING PHENOMENA
OF UNSTIFFENED CIRCULAR CYLINDERS

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This is the fourth of a series of reports covering an investigation of the general instability problem by the California Institute of Technology. The first five reports of this series cover investigations of the general instability problem under the loading conditions of pure bending and were prepared under the sponsorship of the Civil Aeronautics Administration. The succeeding reports of this series cover the work done on other loading conditions under the sponsorship of the National Advisory Committee for Aeronautics.

INTRODUCTION

This report is to deal primarily with the continuation of tests of sheet-covered specimens and studies of the buckling phenomena of unstiffened circular cylinders. The earlier work on this investigation of the problem of general instability of stiffened metal cylinders at C.I.T. has been reported in references 1, 2, and 3. Tests have been completed on the first series of sheet-covered specimens. The longitudinals and frames of the sheet-covered specimens were identical to those of the wire-braced specimens discussed in reference 3. The sheet covering was in all cases 0.010-inch 17S-T dural. The longitudinal spacing was varied from 2.53 to 10.12 inches and the frame spacing from 1 to 16 inches. An attempt has been
made to correlate the experimental data of the wire-braced and sheet-covered specimens. A detailed discussion is given in the discussion of the normal restraint coefficient in this report. Ryder's theoretical work has been applied to three specimens. The results are tabulated in table III and discussed in the body of the report.

In addition to the results on the sheet-covered specimens, the results of an investigation on axially loaded thin-wall metal cylinders will be included in this report. As the preliminary work of this investigation was discussed in reference 2, only results of the more recent work are included. An important finding of this investigation has been the determination of the initial wave form. It has been found that the initial wave form does not agree with the uniform sinusoidal type of wave which has been previously assumed for the theoretical solution, but is elliptical in shape, scattered at random through the cylinder, and changes to a diamond shape as the load is increased.

**EXPERIMENTAL INVESTIGATION OF SHEET-COVERED SPECIMENS**

As pointed out in reference 2, a number of sheet-covered specimens were to be tested to determine whether or not a correlation could be obtained between the failing bending moments of the wire-braced and the sheet-covered specimens. The construction of the sheet-covered and wire-braced specimens was essentially similar, the only difference being that the wire bracing was replaced by the sheet. Details of construction and test procedure have been discussed in detail in reference 2 and will not be repeated here.

Table I gives the complete set of sheet-covered specimens which have been tested, the number of frames and longitudinal in each specimen, the failing bending moment, the critical compressive longitudinal stress, and the restraint coefficient. Specimens 25 to 28 were discussed in reference 3, and specimens 29 to 39 have been tested since that report was written.

Specimen 29 failed by panel instability; the tabulated compressive stress is that at which buckling between frames started and corresponds to a moment of 66,000 inch-pounds. Because of the symmetrical buckling of the longitudinal, transverse stresses were set up in the sheet.
As the amplitudes of the longitudinals increased, the transverse stresses became larger and the stabilizing effect of the sheet increased. This stabilizing effect of the sheet on the longitudinals was quite evident at the higher loads, as illustrated in figures 2 and 38, and prevented collapsing of the specimen. The bending moment was increased to 123,000 inch-pounds without any definite failure. Specimens 28 and 34 started to fail by panel instability; however, upon increasing the bending moment the frames failed at the tabulated bending moment. The loads at which panel instability occurred were 140,000 and 45,000 inch-pounds, respectively.

In figure 4 the compressive failing stress, which is discussed later, is plotted as a function of the longitudinal spacing $b$, for constant values of $d/b$, referred to as "aspect ratio." It is of considerable interest to note that each curve is displaced by a contraction or expansion of the abscissa. The regularity of this family of curves would indicate that such a parameter exists that if the compressive stress is plotted as a function of this parameter a single curve would be obtained. If such a parameter can be found, a limiting value could be established which would indicate the transition region between panel instability and general instability. A number of parameters have been attempted, but as yet the results have not been very successful. In figure 37 the failing compressive stress has been plotted as a function of $\sqrt[3]{\frac{f}{d/b}}$ the parameter suggested by Douch's work. (See reference 1, p. 12). The resulting curve indicates a linear relationship.

In calculating $I_{\sigma_t}$ and $I_{\sigma_f}$, the following assumptions were made:

1. The effective width of sheet acting with each longitudinal can be calculated by Marguerre's equation,

$$\frac{W_e}{b} = \frac{1}{2} \sqrt{\frac{\sigma_t}{\sigma}}$$

where

- $\sigma_t$ longitudinal stress
- $\sigma_b$ buckling stress of sheet
2. The effective width of sheet acting with the frame is equal to the effective width of sheet acting with the longitudinal.

\[ I_\sigma \]

is then the moment of inertia of the longitudinal plus an effective width of sheet corresponding to the longitudinal stress \( \sigma \), and \( I_{\sigma f} \) is the moment of inertia of the frame plus an effective width of sheet equal to that acting with the longitudinal. In view of these rather arbitrary assumptions, too much confidence should not be placed in this curve until further investigations have been carried out on the effects of changing the sheet thickness, and the stiffness of the frames and the longitudinals.

Ryder's analysis could be applied only to three specimens: namely, 25, 26, and 27, as the parameters of the other specimens lie outside the range covered by the published charts. The results for these three specimens are given in table III. In all three cases the calculated panel instability stress is larger than the calculated general instability stress; hence the method predicted correctly the occurrence of general instability. The predicted instability stress and the experimental value are in good agreement for specimen 27; for specimens 25 and 26 the predicted stresses are considerably lower than the experimental stresses.

An extensive comparison between the theoretically predicted general instability stresses and the experimentally obtained stresses will be given after tests have been conducted on specimens in which the sheet thickness and the stiffness of the frames and the longitudinals have been varied.

**MAXIMUM STRESSES IN THE LONGITUDINALS**

In the first sheet-covered specimens an attempt was made to measure the stresses in the longitudinals with Huggenberger extensometers. The stress measurements as indicated by the curves in figures 13 to 16 have not been very successful. Various methods of attaching the instruments to the longitudinals have been tried; however, the irregularity of the stress measurements has not been eliminated. A method of measuring the maximum stresses which has been adopted is to measure the over-all maximum
deflections of the specimen by means of dial gages, as shown in the photographs (figs. 3 and 38 to 47). If the elastic modulus of the longitudinals and the over-all strain are known, the stresses can be calculated. Since the radial deflections of the stiffeners are measured for various increments of load, the maximum stress can be correctly calculated, even for cases in which radial deflection occurs, by means of the equation

\[ \sigma = \frac{\Delta L E}{L} - \frac{E}{2L} \int_0^L \left( \frac{\partial w}{\partial x} \right)^2 \, dx \]

where

- \( \sigma \) stress, pounds per square inch
- \( \Delta L \) total over-all deflection, inches
- \( L \) length of the specimen, inches
- \( w \) radial deflection, inches

The expression \( \frac{E}{2L} \int_0^L \left( \frac{\partial w}{\partial x} \right)^2 \, dx \) is the correction for the deflection caused by the wave form of the longitudinals. It has been found that, in general, the correction due to the curvature (M/EI) is quite small; however, for cases in which the longitudinals buckle between frames, the correction becomes quite appreciable. These corrections were made in the measured over-all deflections of specimen 34. The results of this latter type of stress measurement are shown in figures 8 to 12, in which the stress is plotted as a function of the applied bending moment. It is felt that these results are more reliable than those obtained from the extensometer readings. One disadvantage is that only the maximum stresses are measured; however, in the majority of cases only the maximum stresses are of primary importance.

The compressive stress curve in figure 12 is rather interesting in that three definite breaks occur in the curve. It seems logical to assume that the first break is due to buckling of the sheet between longitudinals,
the second to buckling of the sheet between rivets, and the third to the stress exceeding the proportional limit of the material.

A new method of calculating the actual stress which occurs in the longitudinals of stiffened cylinders subjected to pure bending has been recently developed by R. L. Cox (reference 4). Stress calculations based on this method are in excellent agreement with the above-described measured stresses. The tabulated stresses for specimens 25, 26, and 28 were not measured but merely calculated by this method; the stress for specimen 28 was calculated on the basis of 168,000 inch-pounds bending moment, assuming no buckling of the longitudinals.

THE NORMAL RESTRAINT COEFFICIENT P/δ

The resistance of a stiffened cylinder to an externally applied radial load has been discussed in detail in reference 3. As stated in the concluding remarks, further experimental evidence was necessary to establish the validity of $P/\delta$ as a correlation parameter for the wire-braced and sheet-covered specimens. It was also thought that this parameter might aid in predicting the failing load of a specimen without applying any load to the structure other than the loads necessary to obtain the $P/\delta$ values. A plot of failing bending moment as a function of $P/\delta$ for all the sheet-covered specimens and for a number of the wire-braced specimens is shown in figure 5. This plot indicates that the expected general relationship does not hold, inasmuch as the failing bending moment is not only a function of $P/\delta$ but also varies with the longitudinal spacing. The linear relationship, however, holds between certain limits. For the sheet-covered specimens, the relation is linear with the exception of the 1-inch frame spacing, which is an extreme case and can hardly be expected to conform. For the wire-braced specimens the relationship is, in general, nonlinear. It should be noted that for the 5.06- and 10.12-inch longitudinal spacing the values of $P/\delta$ differ by only a few percent. To investigate further the effect of longitudinal spacing, the $P/\delta$ value was obtained for a specimen in which the longitudinal spacing was 50.6 inches — that is, only the top and the bottom longitudinals remained. The curves of $P$ against $\delta$ for this specimen and for a specimen having a 10.12-inch longitudinal spacing
are shown in figure 7. The difference in the initial slopes—that is, \( P/\delta \), is only 5 percent. The small difference which exists in the \( P/\delta \) value as the spacing of the longitudinals is varied from 5.06 to 50.6 inches leads to the conclusion that after a certain longitudinal spacing, lying between 2.53 and 5.06 inches, \( P/\delta \) is no longer a measure of the resistance of the specimen as a whole to an externally applied load but rather the resistance of a single longitudinal. The critical longitudinal compressive stress has also been plotted as a function of \( P/\delta \) in figure 6. Only the sheet-covered specimens having a 2.53- and a 5.06-inch longitudinal spacing scatter around a common curve.

There are, therefore, two difficulties in using \( P/\delta \) as a correlation parameter for the failing moment:

1. It is evident that the elastic characteristics of the stiffened cylinder are determined by the longitudinal and the circumferential stiffnesses. The measurement of \( P/\delta \) gives only something like the mean stiffness in these two directions. If the failing moment is a function of the same mean stiffness, then the failing moment will be a function of \( P/\delta \) only. If this is not true, then some other parameter like \( d/b \) (aspect ratio of stiffening) must be used with \( P/\delta \). This is confirmed by the experiments, as shown in figure 5.

2. It is also evident from figure 5 that the value of \( P/\delta \) changes very slowly when the longitudinal spacing is large, while the failing moment changes very rapidly. Thus the failing moment against \( P/\delta \) curve, at a constant \( d/b \) ratio, is very steep when the longitudinal spacing is large. Therefore, a small error in the \( P/\delta \) determination gives a large error in the failing moment. It should, however, be kept in mind that the 10-inch longitudinal spacing is already considerably larger than that which would be encountered in practice for geometrically equal structures.

At present, there is no evidence of a reasonable correlation parameter between the sheet-covered and the wire-braced specimens, and it probably will be necessary to continue the experimental work with sheet-covered specimens.
DEFLECTION OF THE LONGITUDINALS

The deflection curves of the longitudinals, after failure of the specimen, are shown in figures 17 to 34. A marked difference has been observed in the type of failure of the wire-braced and sheet-covered specimens. Failure of the wire-braced specimens was in general a gradual process — that is, the specimens tend to approach a maximum bending moment in an asymptotic manner. The failure, however, of the sheet-covered specimens is characterized by a sudden and violent collapsing of the specimen. The radial deflection of the longitudinals, for longitudinal spacings less than 16 inches, is practically zero up to the failing load. A number of photographs (figs. 38 to 47) also are included to illustrate further the failure pattern of the longitudinals and the frames.

EXPERIMENTAL INVESTIGATIONS ON COMPRESSIVE FAILING STRESS OF UNSTIFFENED CIRCULAR CYLINDERS

In the discussion of the strength of axially loaded, unstiffened cylinders (reference 1) it was pointed out that a very poor agreement exists between experimental results and those calculated by the classical buckling theories for circular cylinders. This was especially true for large values of $R/t$. It was also found that very little information was available on the effect of length, particularly for values of $L/R < 1$.

In view of the need for additional information concerning those two parameters a systematic investigation was carried out on steel cylinders in which the $R/t$ ratios were higher than had been previously investigated and on cylinders whose lengths were less than the radius. The specific parameters involved in this investigation were:

1. the radius-thickness ratio $R/t$
2. the length-radius ratio $L/R$
3. the critical stress-elastic modulus ratio $\sigma/E$
The specimens tested were all fabricated from standard shim stock steel in which the nominal thickness was varied from 0.002 to 0.009 inch. Since the fabricated cylinders had a radius of 6.375 inches the \( R/t \) range varied from 750 to 3000. The \( L/R \) ratio was varied from 0.1 to 1.5.

The ends of the test cylinder were rigidly clamped into steel end plates, giving fixed end support to the axial fibers of the cylinder. The test apparatus is shown in figures 48 and 49. The load was applied by means of the screw jack and transmitted through the ring, which measures the load, to the cylinder. To prevent any horizontal components of load, the ring was mounted on a spherical ball joint.

The test results are shown in figures 35 and 36, in which \( \sigma/E \) is plotted as a function of \( L/R \) for constant values of \( R/t \).

where

\[
\sigma \quad \text{failing stress, pounds per square inch} \\
E \quad \text{Young's modulus, pounds per square inch}
\]

An empirical equation was developed to fit the experimental points. The equation is essentially of the same form as the Wagner empirical design formula (reference 5), inasmuch as the variables used are \( t/R \) and \( t/L \); however, the coefficients and exponents have been modified to read:

\[
\frac{\sigma}{E} = 9(t/R)^{1.8} + 0.16(t/L)^{1.3}
\]

A plot of this equation for values of \( R/t \) and \( L/R \) corresponding to the range of the experimental investigation is shown by the curves in figures 35 and 36. For values of \( L/R \) greater than 1.5 experimental results indicate that \( \sigma/E \) is for all practical purposes a constant.

These experimental results are again at variance with the theoretical investigation of W. Flügge as cited by S. Timoshenko. (See reference 1.) The classical theory of W. Flügge shows that the length effect is negligible
until \( L/\pi R \) is lower than 0.2, where \( m \) is the number of half-waves in the axial direction. Since the edges of the test specimens were clamped, it is evident that \( m = 2 \) for the short cylinders. According to the classical theory, therefore, the length effect is negligible until \( L/R \) is less than 0.4. This is another failure of the classical theory of thin shells to predict correctly the behavior of buckling phenomena.

Since the physical properties of the shim stock varied for every thickness, it was necessary to determine experimentally the modulus of elasticity for each thickness. The results are tabulated in table II. The stress-strain relation was obtained for the material in tension; the tension load was applied, with reference to the grain structure of the material, in the same direction as the compression load in the test cylinder.

DETAILED STUDY OF BUCKLING PHENOMENA
OF CYLINDRICAL SHELLS

The relatively large discrepancies between the theoretically predicted and the experimentally obtained buckling loads have led to the conclusion that some of the assumptions made in the theoretical treatment of the problem may be at variance with the actual conditions. Hence, to obtain a better understanding of the mechanism involved in the failure of thin-wall cylinders, it was felt that it would be desirable to determine the exact shape of the initial waves which appear in the test cylinder. This was accomplished by restraining the loading mechanism so that any desired over-all deflection could be maintained at any stage of the loading.

The test apparatus is shown in figures 50 to 52. The three upper set screws afford adjustment of the loading head and rest on a \( 3/4 \)-inch plate. This plate, in turn, is held in position by three \( 1/2 \)-inch screws resting on the base plate and turned by means of the gear system shown. This lowers or raises the \( 3/4 \)-inch plate as desired. The small \( 2 \)-inch central gear, which turns the three \( 5 \)-inch diameter gears, can be externally operated. In this manner the motion of the loading head can be arrested at any desired position during loading of the specimen.
The progressive change in the wave shape and the wave pattern is indicated in figures 53 to 64. The first specimen, designated as C-1 to C-6 in the figures, was 9 inches long with a 0.0034-inch wall thickness. The second specimen, C-8 to C-13, was 6 inches long with a 0.0034-inch wall thickness.

It should be noted that the wave pattern does not agree with the uniformly distributed sinusoidal type of wave which has been previously assumed for the theoretical solution. The initial wave form is elliptical in shape and scattered at random through the specimen. As the load is increased, the waves tend toward a diamond shape and move to a more uniform configuration. The discrepancy between the actual and the assumed wave form may account for the large difference in the theoretically predicted and the experimentally obtained buckling load.

Guggenheim Aeronautical Laboratory,
California Institute of Technology,
Pasadena, Calif., September 1939.

REFERENCES


<table>
<thead>
<tr>
<th>Test</th>
<th>Longitudinal spacing, b (in.)</th>
<th>Frame spacing, d (in.)</th>
<th>Number of frames in 64 in.</th>
<th>P/8</th>
<th>Failing moment M.B. (in.-lb)</th>
<th>Max. compressive stress at failure</th>
<th>Type of failure</th>
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<tr>
<td>25</td>
<td>2.53</td>
<td>8</td>
<td>7</td>
<td>330</td>
<td>219,000</td>
<td>16,200</td>
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<td>26</td>
<td>2.53</td>
<td>4</td>
<td>15</td>
<td>1450</td>
<td>274,000</td>
<td>19,400</td>
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<td>2</td>
<td>31</td>
<td>614</td>
<td>379,000</td>
<td>25,600</td>
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<td>2.53</td>
<td>16</td>
<td>3</td>
<td>255</td>
<td>168,500*</td>
<td>13,000</td>
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<tr>
<td>29</td>
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<td>16</td>
<td>3</td>
<td>222</td>
<td>123,000*</td>
<td>6,600**</td>
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<td>5.06</td>
<td>8</td>
<td>7</td>
<td>257</td>
<td>107,500</td>
<td>12,200</td>
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<td>4</td>
<td>15</td>
<td>350</td>
<td>137,500</td>
<td>16,500</td>
<td>Do.</td>
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<td>2</td>
<td>31</td>
<td>510</td>
<td>185,000</td>
<td>22,200</td>
<td>Do.</td>
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<td>10.12</td>
<td>16</td>
<td>3</td>
<td>209</td>
<td>50,000</td>
<td>8,200</td>
<td>Started by panel instability - final failure general instability.</td>
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<td>10.12</td>
<td>8</td>
<td>7</td>
<td>261</td>
<td>60,000</td>
<td>10,500</td>
<td>General instability.</td>
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<td>10.12</td>
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<td>15</td>
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<td>63</td>
<td>740</td>
<td>209,000</td>
<td>26,000</td>
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<td>63</td>
<td>815</td>
<td>397,000</td>
<td>29,600</td>
<td>Do.</td>
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*Failing bending moment.  
**Panel instability stress.
# TABLE II

**VARIATIONS OF YOUNG'S MODULUS WITH THICKNESS**

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<tr>
<th>Nominal thickness (in.)</th>
<th>Young's modulus (lb/sq in.)</th>
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<tr>
<td>0.002</td>
<td>$33.5 \times 10^6$</td>
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<td>0.003</td>
<td>32.0</td>
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<tr>
<td>0.004</td>
<td>32.4</td>
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<tr>
<td>0.005</td>
<td>31.5</td>
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<td>0.006</td>
<td>30.6</td>
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<td>0.0085</td>
<td>29.0</td>
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# TABLE III

CALCULATION OF CRITICAL STRESS BY RYDER'S METHOD

FOR SHEET-COVERED SPECIMENS

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Longitudinal spacing ( b ) (in.)</th>
<th>Frame spacing ( d ) (in.)</th>
<th>Max. compressive stress at failure, ( \sigma_{cr} ) (( \sigma_{cr} \text{ exp} ))</th>
<th>( \frac{I_{cr}}{I_{cr}} )</th>
<th>( \frac{I_{cr}}{I_{cr}} )</th>
<th>( K_1 )</th>
<th>( K_2 = \frac{I_{cr}}{K_1 I_{cr} d} )</th>
<th>( K_3 = \frac{A_{cr}}{K_1 A_{cr} d} )</th>
<th>( K_4 = \frac{G' tb}{MK_1 A_{cr}} )</th>
<th>( t_0 / \rho_b ) (from Ryder's curves)</th>
<th>Calculated critical stress (lb/sq in.)</th>
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</thead>
<tbody>
<tr>
<td>27</td>
<td>2.53</td>
<td>2</td>
<td>25,600</td>
<td>6.40</td>
<td>1.29</td>
<td>1.30</td>
<td>0.0541</td>
<td>0.915</td>
<td>0.101</td>
<td>0.50</td>
<td>22,290</td>
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<tr>
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<td>2.53</td>
<td>4</td>
<td>19,400</td>
<td>5.88</td>
<td>1.29</td>
<td>1.30</td>
<td>0.0270</td>
<td>0.922</td>
<td>0.100</td>
<td>0.30</td>
<td>13,380</td>
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<tr>
<td>25</td>
<td>2.53</td>
<td>8</td>
<td>16,200</td>
<td>5.40</td>
<td>1.30</td>
<td>1.30</td>
<td>0.0135</td>
<td>0.917</td>
<td>0.100</td>
<td>0.18</td>
<td>8,410</td>
</tr>
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</table>
NOTE:
All figures are four times actual size

STIFFENER - S

\[
\text{AREA} = 0.0324 \, \text{sq.in.} \\
I_{xx} = 0.000374 \, \text{in.}^4
\]

FRAME - F

\[
\text{AREA} = 0.0291 \, \text{sq.in.} \\
I_{xx} = 1.557 \times 10^{-5}
\]
FIGURE 2
Deflection pattern of longitudinals causing transverse stresses to be set up in the sheet.

FIGURE 3
Diagram showing measurement of overall axial deflection.
Critical Longitudinal Stress as a Function of the Longitudinal Spacing - d
for constant values of \( \% \)

\( d = \text{Frame Spacing} \)

Critical Longitudinal Stress \( \times 10^3 \) - Lbs./Square Inch

Longitudinal Spacing - Inches

Panel Instability

Fig. 4
Failing Bending Moment
As a Function of \( \frac{P}{h} \)
At Zero Bending Moment

Lines of Constant Aspect Ratio \( \frac{D}{h} \)

Radius of Cylinder, 15.76\(^\circ\)

Normal Restraint Coefficient \( \frac{P}{D} \) ~ 185/lb

Fig. 5
Fig. 6

NORMAL RESTRAINT COEFFICIENT - \( \frac{\pi}{6} \) - LBS/INCH

2.53" LONGITUDINAL SPACING
5.06" WIRE BRACING
10.12" SHEET COVERING

Fig. 6
Radial Deflection as a Function of Applied Load - P

Tests #36, #36A

0.10" Longitudinal Spacing
4.50"

4" Frame Spacing For Both

Fig. 7
Fig. 8

Maximum Longitudinal Stress
As a Function of
Bending Moment

Test #27

Tension
Compression

Bending Moment (in lbs.

Maximum Longitudinal Stress (in psi)

Fig. 8
Maximum Longitudinal Stress - Test #32
as a function of Bending Moment

Maximum Longitudinal Stress - 185 (50) inch

Fig. 9
Maximum Longitudinal Stress as a Function of Bending Moment

Maximum Longitudinal Stress = 185/50 inch

Fig. 10
Maximum longitudinal stress as a function of bending moment

Test #38

- Tension
- Compression

Maximum longitudinal stress ~ 1 lb/50 inch

Fig. 11
Maximum Longitudinal Stress as a Function of Bending Moment

Test 38

Bending Moment - Inch Lbs

Tension

Compression

Maximum Longitudinal Stress - Lbs/Inch

Fig. 12
TEST "25"

Stresses in the Longitudinals as a Function of the Applied Bending Moment

Stress in lbs/Inch

Fig 13
Test of 25
Stresses in the longitudinal axis as a function of the applied bending moment

Fig. 14
Test #25
Stresses in the Longitudinals as a function of the Applied Bending Moment.
Test #25
Stresses in the Longitudinals as a Function of the Applied Bending Moment

Bending Moment in Inch-Lbs

Stress in lbs/sq inch

Fig. 16
Fig. 17

Radial Deflection
At Failure
40 Conditionals
7 Frames
Fig. 19
TEST 26
DEFLECTION OF LONGITUDINALS
40 LONGITUDINALS

FRAMES:
10°
10°
10°
10°
10°
TEST 26

DEFLECTION OF LONGITUDINALS

40 LONGITUDINALS
Fig. 23

Test No. 27

Deflection of Longitudinals

0 Longitudinals

Frames

0°

15°

10°

Fig. 23
TEST 28

DEFLECTION OF LONGITUDINALS

FRAME 6

FRAME 5

FRAME 4

FRAME 3

FRAME 2

FRAME 1

Fig. 24

NACA Technical Note No. 908
TEST 29
DEFLECTION OF LONGITUDINALS
20 LONGITUDINALS

FRAMES

Fig. 25
TEST 30

DEFLECTION OF LONGITUDINALS

10 LONGITUDINALS

Fig. 26
TEST 91
DEFLECTION OF LONGITUDINALS
20 LONGITUDINALS

FRAMES

Fig. 27
TEST No. 32
DEFLECTION OF LONGITUDINALS
FRAMES

\( \gamma = 36^\circ \)

\( \gamma = 18^\circ \)

\( \gamma = 0^\circ \)

\( \gamma = 24^\circ \)

\( \gamma = 342^\circ \)

\( 10^\circ \)

64°
TEST *34

DEFLECTION OF LONGITUDINALS

10° LONGITUDINALS
TEST 75
DEFLECTION OF LONGITUDINALS
10. LONGITUDINALS
TEST #38

DEFLECTION OF LONGITUDINALS
2.0 LONGITUDINALS

ONE INCH FRAME SPACING

Fig. 34
COMPRESSION TEST OF CIRCULAR CYLINDERS

LENGTH EFFECT

$\frac{f}{E} \text{ vs } \frac{L}{R}$

EXPERIMENTAL POINTS
WITH EMPIRICAL
DESIGN FORMULA

$E = 9(\frac{R}{L})^6 + 16(\frac{L}{R})^{1/3}$

LIMITS OF $\frac{L}{R} < 15$

FOR $\frac{L}{R} > 15$ ASSUME CONSTANT

Fig. 35
COMPRESSION TEST OF CYLINDERS

LENGTH EFFECT

$E \text{ vs. } L$

EXPERIMENTAL POINTS
WITH EMPIRICAL
DESIGN FORMULA

$E = 9(L)^{1/6} + 1.5(L)^{1/3}$

LIMITS $0.1 < L < 1.5$

FOR $L > 1.5$ ASSUME CONSTANT

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Fig. 36
Fig. 37

Maximum Compression Stress - L/s/0.616 Arch

253° Longitudinal Spacing
+ 5.06° 
+ 10.12°

Panel Instability

\[
\left( \frac{I_{ef}}{d} \right) \times \frac{I_{es}}{b}
\]

Fig. 37
Fig. 48
Test Apparatus with Specimen in Position.

Fig. 49
Assembled Cylinder

Fig. 50
Head Lowering Mechanism.

Fig. 51
Gear System

Fig. 52
Loading Apparatus